# Retrieval of Snow Grain Size and Impurity from GLI: Atmospheric Correction

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# **OUTLINE OF TALK**

- Brief Overview of Theoretical Aspects and Retrieval Principles:
   => Which GLI Channels Do We Use and Why?
   Short Description of Detrieval Dreadows
  - => Short Description of Retrieval Procedure.
- Atmospheric Correction and Retrieval Products:
  - => Cloud Mask
  - => Aerosol Model and Optical Depth
  - => Snow Grain Size and Impurities
  - => Spectral Snow Albedo
- Algorithm Testing and Validation:
  - => Use of Synthetic Data Numerical Testbed
  - => Testing Against MODIS Data
  - => Field Validations Ultimately Required
- Summary



#### Theoretical Aspects and Retrieval Principles (1)

Our algorithm development is based on:

• the discrete-ordinate-method (DISORT) [see Refs. 2-4] to compute the top-of-the-atmosphere (TOA) radiances, because:

=> this method allows radiances to be computed at arbitrary userspecified polar and azimuthal angles.

We expand the phase function as:

$$p(\tau, \cos \Theta) = p(\tau, u', \phi'; u, \phi) = \sum_{m=0}^{2M-1} (2 - \delta_{0,m}) p^m(u', u) \cos m(\phi' - \phi) \quad (1)$$

 $p^{m}(u',u) = \sum_{l=m}^{2M-1} (2l+1)g_{l}(\tau)\Lambda_{l}^{m}(u')\Lambda_{l}^{m}(u); \Lambda_{l}^{m}(u) = \sqrt{(l-m)!/(l+m)!}P_{l}^{m}(u);$ 

 $g_l(\tau) = \frac{1}{2} \int_{-1}^{+1} P_l(\cos \Theta) p(\tau, \cos \Theta) d(\cos \Theta); \tau$  is the vertical optical depth;  $(u' = \cos \theta', \phi')$  and  $(u = \cos \theta, \phi)$  are the cosine of the polar angle and the azimuthal angle, before and after the scattering, respectively.



Theoretical Aspects and Retrieval Principles (2)

• Since Eq. (1) is a Fourier cosine series, we expand the radiance in the same way:

$$I(\tau, u, \mu_0, \Delta\phi) = \sum_{m=0}^{2M-1} I^m(\tau, u, \mu_0) \cos(m\Delta\phi)$$
(2)

 $-\mu_0 = cos\theta_0$  is the cosine of the solar zenith angle  $\theta_0$ 

- $-\Delta \phi = \phi_0 \phi$  is the relative azimuth angle between the incident solar beam direction  $\phi_0$  and the sensor viewing direction  $\phi$
- $-I(\tau,\mu_0,u,\Delta\phi)$  is the radiance
- $-I^m(\tau,\mu_0,u)$  is the *m*-th Fourier component of the radiance
- Each Fourier component satisfies the radiative transfer equation:  $I^m(\tau, u, u_0) = a(\tau)$

$$u\frac{I^{-}(\tau, u, \mu_{0})}{d\tau} = I^{m}(\tau, u, \mu_{0}) - \frac{u(\tau)}{2} \int_{-1}^{1} p^{m}(u, u') I^{m}(\tau, u') du' - Q^{m}(\tau, u) \quad (3)$$

• Solution of Eq. (3) for each m yields  $I^m(\tau, u, \mu_0)$ , and substitution in Eq. (2) yields  $I(\tau, u, \mu_0, \Delta \phi)$ .



Theoretical Aspects and Retrieval Principles (3)

- We store the  $I^m(\tau, u, \mu_0)$  terms [see Eq. (2)] in the lookup table.
- The TOA radiance  $I(\tau, u, \mu_0, \Delta \phi)$  is then computed based on Eq. (2) using an interpolation method.
- We employ a *cubic spline interpolation* method [see Ref. 5] for the polar and solar zenith angle dependence of the radiance.
- Use of Eq. (2) implies an accurate analytic treatment of the azimuth dependence of the radiance.



#### Reflected radiances in Channels 5 and 26



Figure 1: Reflected radiances in channels 5 and 26 as a function of mass fraction of soot and grain size.

#### Flow Chart of Retrieval Algorithm



Figure 2.2 Flow chart of the retrieval algorithm for snow grain size and impurity concentration.  $\tau_a$  is the aerosol optical depth, Rs the snow grain size, and  $m_F$  the impurity concentration. The  $\rho_{sat}(26)$ ,  $\rho_{sat}(19)$ , and  $\rho_{sat}(5)$  are the satellite-measured reflectances at GLI channels 26, 19 and 5, respectively. The  $\rho_{mod}(19)$  is the computed reflectance (from lookup table) at GLI channel 19.



Figure 2: Histograms of retrieved snow grain size from AVIRIS channels 54, 73, 93, and 145.

#### Atmospheric Correction (1)

Atmospheric Correction means Removal of Aerosol Contribution to TOA Radiance, because:

- Rayleigh scattering can be computed accurately;
- absorption by trace gases is unimportant in channels 1 and 5. Removal of the aerosol contribution to TOA radiance is difficult:
- large spatial and temporal variation in aerosol properties
- high albedo of snow surface.
- Use of incorrect aerosol model implies TOA reflectance errors:
  - as large as 20% for weakly-absorbing aerosols;
  - an error of 50% or more for strongly absorbing aerosols.
- Such large errors will cause a failure of the retrieval of snow grain size and impurity.
- Proper selection of aerosol model is critically important for accurate retrieval of snow grain size and impurity.

#### Atmospheric Correction (2)



Figure 3: Relative deviations in TOA reflectance in GLI channels 5 and 19 resulting from use of wrong aerosol models. The right panels contain the input grain size and impurity for each test pixel.

#### Atmospheric Correction (3)

How Can We Do Atmospheric Correction over Bright Surfaces like Snow? The Answer is:

- the reflectance in channel 5 decreases almost linearly with optical depth when the albedo is higher than about 0.5;
- Note also that:
- the reflectance in channel 5 *increases* almost linearly with optical depth when the albedo is *lower* than about 0.5.
- Hence:
- Aerosol Removal is Feasible over Bright as Well as Dark Surfaces!!



#### Atmospheric Correction (4)



Figure 4: TOA reflectance at GLI channel 5 as a function of aerosol optical depth and surface reflectance. (a): non-absorbiing aerosols; (b): absorbing aerosols.

#### Atmospheric Correction (5)

For a Lambertian surface the reflectance is given exactly by:

$$\rho_{tot}(\theta_v, \rho_{sur}) = \rho_{atm}(\theta_v, \rho_{sur} = 0) + \frac{\rho_{sur} \cdot \mathcal{T}(\theta_s) \cdot \tilde{\mathcal{T}}(\theta_v)}{\pi (1 - \rho_{sur} \cdot \overline{\tilde{\rho}})}.$$
(4)

where

- $\theta_s = \text{solar zenith angle}; \quad \theta_v = \text{polar viewing angle};$
- $\mathcal{T}(\theta_s) = \text{diffuse transmittance for illumination of the atmosphere from$ *above* $;}$
- $\tilde{\mathcal{T}}(\theta_v)$  = diffuse transmittance for illumination of the atmosphere from *below*;
- $\overline{\tilde{\rho}}$  = spherical albedo for illumination of the atmosphere from *below*;

Solving for  $\rho_{sur}$ , we find:

$$\rho_{sur} = \rho_c / (1 + \rho_c \cdot \overline{\tilde{\rho}})$$
(5)

where

 $\rho_c = \pi [\rho_{tot} - \rho_{atm}] / \mathcal{T}(\theta_s) \cdot \tilde{\mathcal{T}}(\theta_v).$ 



#### Atmospheric Correction (6)



Figure 5: Retrieved Lambertian albedo  $\rho_{sur}$  as a function of aerosol optical depth [(a) and (b)], and as a function of aerosol model [(c) and (d)].

#### Atmospheric Correction (7)



Figure 6: TOA reflectance  $\rho_{tot}$  as a function of aerosol optical depth for model "average-continental" (RH = 70%). (a): snow grain size = 200  $\mu$ m and snow impurities (from top to bottom): 0.02, 0.05, 0.1, 0.2, 0.5, 1.0, 1.5 2.0, 2.5 × 10<sup>-6</sup> ppmw (parts per million by weight). (b): snow impurity = 0.2 × 10<sup>-6</sup> ppmw and snow grain size (from top to bottom): 50, 100, 200, 500, 1000, 2000  $\mu$ m.



Figure 2.9 Flow chart of aerosol model and aerosol optical depth retrieval.  $\rho_{tot}(1)$  and  $\rho_{tot}(5)$  are the TOA reflectances of GLI channels 1 (0.38  $\mu$ m) and 5 (0.46  $\mu$ m), respectively.  $\rho_{sot}(1)$  and  $\rho_{sot}(5)$  are the Lambertian surface albedo values at GLI channels 1 and 5, respectively. The  $\tau_{s1}$  and  $\tau_{s3}$  are the aerosol optical depth  $\tau$  (0.86) retrieved from GLI channels 1 and 5, respectively, and n is the total number of candidate aerosol models.

### Validation – Synthetic Data (1)



Figure 7: The structure of the GLI image.

# Validation – Synthetic Data (2)



Figure 8: Aerosol Model. LEFT PANEL: Input data. RIGHT PANEL: Retrieved results.

# Validation – Synthetic Data (3)



Figure 9: Aerosol Optical Depths. LEFT PANEL: Input data. RIGHT PANEL: Retrieved results.

# Validation – Synthetic Data (4)



Figure 10: Snow Grain Size. LEFT PANEL: Input data. RIGHT PANEL: Retrieved results.

### Validation – Synthetic Data (5)



Figure 11: Snow Impurity. LEFT PANEL: Input data. RIGHT PANEL: Retrieved results.

# Validation – Synthetic Data (6)



Figure 12: Retrieval (%). LEFT PANEL: Grain Size. RIGHT PANEL: Impurity.

# MODIS Data –Greenland (1)



Figure 13: LEFT PANEL: Cloud mask. RIGHT PANEL: Aerosol optical depth. Retrieved from MODIS data on June 18, 2000 over Greenland..

# MODIS Data –Greenland (2)



Figure 14: LEFT PANEL: Grain size. RIGHT PANEL: Snow impurity concentration. Retrieved from MODIS data on June 18, 2000 over Greenland.

# MODIS Data – Central United States (1)



Figure 15: LEFT PANEL: Cloud mask. RIGHT PANEL: Aerosol optical depth. Retrieved from MODIS data on November 2, 2000 over United States.

### MODIS Data – Central United States (2)



Figure 16: LEFT PANEL: Grain size. RIGHT PANEL: Snow impurity concentration. Retrieved from MODIS data on November 2, 2000 over United States.

# Summary

In summary:

- We have reviewed the snow grain size and retrieval algorithm with an emphasis on atmospheric correction issues.
- It has been tested against synthetic data and appears to be robust. Application to MODIS data yields reasonable results.
- Testing against field data is necessary when GLI data become available.

These algorithms can be used to provide:

- Cloud mask
- Aerosol optical properties
- Snow grain size and impurites
- Spectral albedo



#### References

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