

**Algorithm Description Ver.1.1 (2016.12.19)**

**Algorithm Description Ver.1.2 (2019.3.31)**

**Algorithm Description Ver.2 (2020.3.31)**

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## **Derivation of the absorption coefficient of Coloured Dissolved Organic Matter (CDOM)**

### **1. Physics of the problem**

The IOP algorithm assumes that the remote sensing reflectance ( $R_{rs}$ ) *just above the sea surface* (denoted by  $z=0+$ , where  $z$  represents a depth), or the water-leaving reflectance ( $\rho$ ), is obtained in prior to its implementation.

The  $R_{rs}$  for a wavelength  $\lambda$  is defined by

$$R_{rs}(\theta_v, \varphi_v, z=0+, \theta_s, \varphi_s, \lambda) = L_w(\theta_v, \varphi_v, z=0+, \theta_s, \varphi_s, \lambda) / E_d(z=0+, \theta_s, \varphi_s, \lambda) \quad (1)$$

where  $L_w$  and  $E_d$  are the radiance and the downward plane irradiance at the observation angle (zenith angle  $\theta_v$ , azimuth angle,  $\varphi_v$ ) and the solar angle (zenith angle  $\theta_s$ , azimuth angle  $\varphi_s$ ). The water-leaving reflectance  $\rho$  can be obtained by  $\rho = \pi R_{rs}$ . Morel and Gentili (1993, 1996) showed that the Eq. (1) can be related to the absorption coefficient  $a_t$  and the backscattering coefficient of the bulk water  $b_{bt}$  by

$$R_{rs}(\theta_v, \varphi_v, z=0+, \theta_s, \varphi_s, \lambda) = R(W, \theta_s, \varphi_s, \lambda) F(\theta_v, \varphi_v, z=0-, \theta_s, \varphi_s, \lambda) [b_{bt}(z=0-, \lambda) / a_t(z=0-, \lambda)] \quad (2)$$

where  $R$  is a transmittance from water to air and  $W$  denotes the wind speed. For convenience, all dependencies of the variables on illumination and observation geometries, depth, wavelength etc in Eq. 2 are omitted hereafter, unless otherwise specified. In addition,  $R \times F$  will be denoted by  $F'$  so that Eq.2 is simplified by

$$R_{rs} = F' [b_{bt} / a_t]. \quad (3)$$

The absorption coefficient of the bulk seawater is decomposed into the absorption coefficients of optically active components. It is a common exercise to define those components as pure seawater ( $a_w$ ), phytoplankton ( $a_{ph}$ ), non-algal particles NAP ( $a_d$ ), and CDOM( $a_g$ ), so that

$$a_t = a_w + a_{ph} + a_{dg} \quad (4)$$

where

$$a_{dg}=a_d+a_g \quad (a_d>0, a_g>0) \quad (5)$$

Among the components,  $a_{ph}$  and  $a_d+a_g(=a_{dg})$ , thus not  $a_d$  and  $a_g$ , can be derived from the SGLI/GCOM-C1 IOP algorithm (see Smyth et al., 2006 as well as ATBD for the IOP algorithm). Hence, we assume that  $a_{dg}$  are known in this document. A practical problem here is to decompose  $a_{dg}$  into  $a_d$  and  $a_g$  to retrieve  $a_g$ .

## 2. Dataset

A global in situ dataset was used (Werdell and Bailey 2005) to derive  $a_g$  from  $a_{dg}$ . Figure 1 shows the data distribution of the dataset.

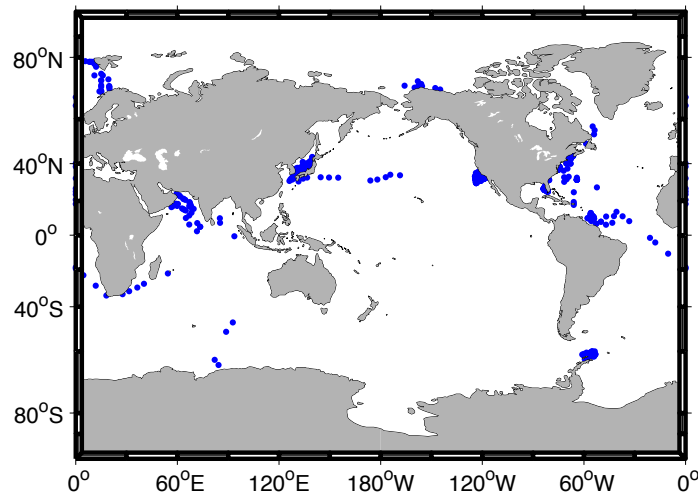


Figure 1 NOMAD data distribution

## 3. Algorithm

The CDOM algorithm here takes the  $a_{dg}$  as an input. Thus, the algorithm decomposes  $a_{dg}$  into  $a_g$  and  $a_d$  in practice. Since the IOP algorithm retrieves  $a_{dg}$  relatively well at shorter wavelengths than other longer wavelengths (Smyth et al., 2006), the former wavelengths will be considered below to derive  $a_g$ . Considering that (i) an optical separation of  $a_g$  from  $a_{dg}$  is challenging as they often have a similar spectrum (IOCCG, 2018) and (ii)  $a_{dg}$  derived from the IOP model would in practice include some uncertainty anyway so that a fuzzy algorithm which can accept input error may be desired, our choice is to derive  $a_g$  from  $a_{dg}$  using an empirical (or statistical) relationship between  $a_g$  and  $a_{dg}$  rather than

using an optical theory: the statistical coefficients can wrap up the above-mentioned uncertainty while bypassing the theoretical challenge. Figure 2 show the empirical relationship between  $a_g$  and  $a_{dg}$  for 412nm obtained from the in situ data. While the simple statistical model of  $a_g=s*(a_{dg})^k$  (i.e. a linear regression model in log-log scale) shows a better  $r^2$ , it also exceeds 1:1 line at smaller end of  $a_{dg}$  so that  $a_g > a_{dg}$  (see a circle in Figure 2). When satellite-derived  $a_{dg}$  is even smaller than the smallest  $a_{dg}$  found in the present in situ dataset (which is likely to happen because a satellite data usually covers a larger spatial domain than in situ observation), a resultant  $a_g$  derived from the fit would violate Eq. 5. Hence, we employ the other statistical model that never exceeds 1:1 line:

$$a_g(411) = \frac{A*a_{dg}(411)}{B+C*a_{dg}(411)} + D \quad (6)$$

where  $A=1.5625$ ,  $B=1.7647$ ,  $C=0.6058$  and  $D=-0.0007218$  which are determined by the least square fit. Although Eq. 6 reduces  $r^2$  statistics by 0.07 (i.e. data variance of 7% is less explained) when compared to the  $a_g=s*(a_{dg})^k$ , also shows a better fit at the higher end of  $a_{dg}$  than  $a_g=s*(a_{dg})^k$  (squared area in Figure 2).

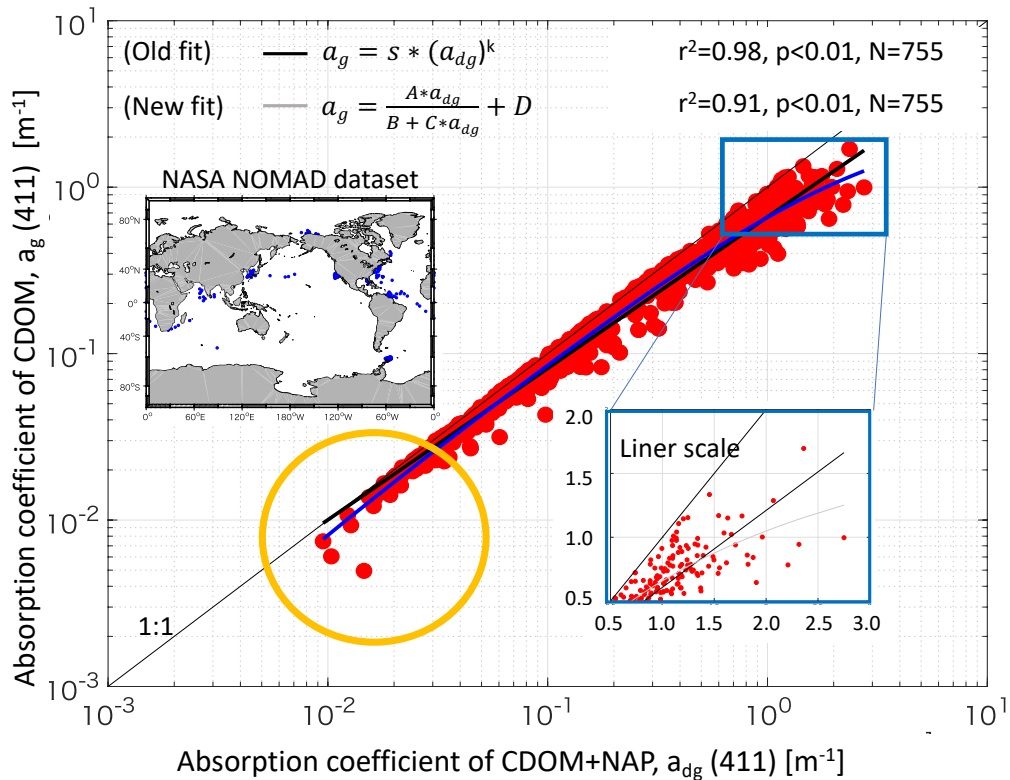


Figure 2. In situ relationship between  $a_g$  (412) and  $a_{dg}$  (411).

Note that Eq. 6 (with the coefficient values mentioned above) leads to  $a_g = -0.0007218 < 0$ , when  $a_{dg} = 0$ . Although this also does not make sense, the value of  $a_g(412) = -0.0007218$  is either lower than detection limit of an instrument or within an uncertainty of the measurement.

Using the actual SGLI/GCOM-C satellite data,  $a_g$  was derived and matched up with  $a_g$  measured in situ (Table 1). Match up was made in such a way that satellite data do not deviate more than +/- 3 hours from the in situ observation time. A 3x3 satellite pixel window is selected (Werdell and Bailey, 2005) so that a pixel nearest to the exact latitude and longitude of an in situ measurement is located at the center of the window, and an average of  $a_g$  within the window is calculated to represent the satellite  $a_g$ . Then the satellite  $a_g$  is compared to the  $a_g$  measured in situ. Although statistical conclusion cannot be drawn due to a lack of a sufficient number of measurements, the differences between the satellite- and in situ  $a_g$  (in linear scale) are between -89.2% and +98.3%.

Table 1

In situ data credit: Profs. Yamashita/Suzuki						
$a_{CDOM(412)}$ [ $m^{-1}$ ]	Date	Latitude	Longitude	Satellite Data (250m/pixel) 3x3 pixels average	In Situ Data	Difference [%]
Old fit	2018.5.27	35.83 ° N	144.00 ° E	0.0294	0.0471	-37.6%
<b>New fit</b>	2018.5.27	35.83 ° N	144.00 ° E	<b>0.0156</b>	<b>0.0471</b>	<b>-66.9%</b>
In situ data credit: Prof. Isada						
Old fit	2018.6.01	45.52 ° N	142.12 ° E	0.1641	0.0633	+159.3%
<b>New fit</b>	2018.6.01	45.52 ° N	142.12 ° E	<b>0.1256</b>	<b>0.0633</b>	<b>+98.3%</b>
In situ data credit: Prof. Isada						
Old fit	2018.6.03	45.41 ° N	145.16 ° E	0.0922	0.0922	+58.3%
<b>New fit</b>	2018.6.03	45.41 ° N	145.16 ° E	<b>0.1110</b>	<b>0.0922</b>	<b>+20.3%</b>
In situ data credit: Prof. Ishizaka						
Old fit	2018.7.20	31.75 ° N	128.16 ° E	0.0253	0.0818	-69.1%
<b>New fit</b>	2018.7.20	31.75 ° N	128.16 ° E	<b>0.0162</b>	<b>0.0818</b>	<b>-89.2%</b>

**Reference:**

Smyth, T. J., G.F. Moore, T. Hirata, J. Aiken, Semianalytical model for the derivation of ocean colour inherent optical properties: description, implementation, and performance assessment, Applied Optics, 45, 8116-8131, 2006.

Werdell, P. J. and S. W. Bailey, An improved in situ data set for bio-optical algorithm development and ocean color satellite validation, Remote Sens. Environ., 98, 122-140, 2005